In-flight calibration of double-probe DC electric field measurements on Cluster

Y. V. Khotyaintsev\textsuperscript{1}, P.-A. Lindqvist\textsuperscript{2}, C. M. Cully\textsuperscript{1,*}, A. I. Eriksson\textsuperscript{1}, and M. André\textsuperscript{1}

\textsuperscript{1}Swedish Institute of Space Physics, Uppsala, Sweden  
\textsuperscript{2}Royal Institute of Technology, Stockholm, Sweden  
*now at: Department of Physics and Astronomy, University of Calgary, Canada

Received: 19 August 2013 – Accepted: 15 January 2014 – Published: 31 January 2014  
Correspondence to: Y. V. Khotyaintsev (yuri@irfu.se)

Published by Copernicus Publications on behalf of the European Geosciences Union.
Abstract

Double-probe electric field instrument with long wire booms is one of the most popular techniques for in situ measurement of DC and AC electric fields in plasmas on spinning spacecraft platforms, which have been employed on a large number of space missions. Here we present an overview of the calibration procedure used for the EFW instrument on Cluster, which involves spin fits of the data and correction of several offsets. We also describe the procedure for the offset determination and present results for the long-term evolution of the offsets.

1 Introduction

Double-probe electric field experiments have been flown on a number of spacecraft (see review by Pedersen et al., 1997) including Cluster (Gustafsson et al., 1997, 2001) and calibration of the DC electric field have always been a challenging and time-consuming task. Main reasons for this are strong influence of the ambient plasma and the spacecraft itself on the measurements. Other techniques to measure electric fields at low time resolution as electron drift instruments and ion spectrometers, such as EDI (Paschmann et al., 1997, 2001) and CIS (Reme et al., 2001) on Cluster, are immune to some of the problems affecting the double-probe measurements, but have their own limitations. With the Cluster Active Archive a semi-automatic approach to in flight calibration of the DC electric field data has been developed (Khotyaintsev et al., 2010) and the purpose of this paper is to describe the main elements of this calibration procedure under nominal operations.

An example of a clear deviation from nominal performance is the non-geophysical electric field detected by EFW due to the wake behind the spacecraft caused by cool (eV) outflowing ionospheric ions drifting at supersonic velocities. Such ions are common in the magnetospheric tail lobes. Careful investigation of this “problem” has resulted in a new method to detect positive low-energy ions, otherwise invisible to de-
tectors on a sunlit spacecraft positively charged to several volts (Engwall et al., 2006, 2009a, b, André and Cully, 2012). However, it is not possible to recover the ambient geophysical electric field in such case.

2 Short instrument description

The detector of the Cluster EFW instrument consists of four spherical sensors numbered 1 to 4 deployed orthogonally on 42.5 m long wire booms in the spin plane of the spacecraft (see Fig. 1). The spacecraft makes one rotation in approximately 4 s. The potential drop between two sensors, separated by 88 m (or 62 m in case of using non-opposing probes) tip-to-tip is measured to provide an electric field measurement. The probe difference signals are normally routed through 10 Hz anti-aliasing low-pass filters if sampled at 25 s$^{-1}$, and through 180 Hz low-pass filters when sampled at 450 s$^{-1}$. The potential difference between each sensor and the spacecraft is measured separately with a sampling frequency of 5 s$^{-1}$ after routing through low-pass filters with a cut-off frequency of 10 Hz. A detailed description of the EFW instrument can be found in Gustafsson et al. (1997, 2001).

3 Calibration procedure

The goal of the calibration procedure is to obtain geophysical DC electric field in the spacecraft spin plane in a despun reference frame. On Cluster we used the ISR2 (Inverted Spin Reference) system, also known as DSI (Despun System Inverted). The $x$ and $y$ axes are in the spin plane, with $X$ pointing as near sunward as possible and $Y$ perpendicular to the sunward direction, positive towards dusk. The $Z$ axis is along the (negative) spacecraft spin axis, towards the north ecliptic. The coordinate system is called “inverted” because the actual spin axis of Cluster is pointing towards the south ecliptic. The ISR2 system thus is identical to GSE if the satellite spin axis angle to
ecliptic north is zero, and is a good approximation to GSE for the usual case of this angle being a few degrees.

3.1 Raw data

The raw data available from EFW under normal circumstances are the two orthogonal electric field components in the spinning frame ($E_{12}$ and $E_{34}$) sampled at 25 of 450 Hz, as well as potentials of the individual probes ($P_1$, $P_2$, $P_3$ and $P_4$) sampled at 5 Hz. In case of probe 1 failure (for dates of permanent failures on C1, C2 and C3 see Lindqvist et. al, 2013), instead of E12 we use E32. Example of raw data is shown in Fig. 2.

As the first stage of calibration it is necessary to perform initial cleaning of the data at which we remove intervals with: bad data due to issues with electronics, probe saturations due to low plasma density (often occurring in in the magnetospheric lobes), and saturations due to non-optimal bias current settings occurring in dense plasmas such as magnetosheath and plasmasphere (Khotyaintsev et. al., 2010). If the spacecraft is in the solar wind we apply a correction for the wakes usually present in the raw data (Eriksson et al., 2007).

3.2 Spin fits

After initial cleaning of the data a spin fitting procedure is performed; the output of this procedure provides basic parameters that are used later in the calibration procedure. In the presence of a constant ambient electric field, the raw data signal (probe potential difference) is a sine wave (see Fig. 2, upper panel) where the amplitude and phase give the electric field magnitude and direction. A least-squares fit to the raw data of the form

$$y = A + B \sin(\omega t) + C \cos(\omega t) + D \sin(2\omega t) + E \cos(2\omega t) + \ldots$$

(1)

is done once every 4 s ($2\pi / \omega \approx 4$ s is approximately the spacecraft spin period).

The standard deviation of the raw data from the fitted sine wave can be used as indication of high frequency variations in the data. Higher order terms, D, E, . . . , may be
used for diagnostics of data quality: normally the higher order terms are much smaller than B and C, and the opposite situation would indicate problems with the measurements.

3.3 Offsets

The sine and cosine terms, B and C after correction for ISR2 offsets provide the 4s (spin) resolution electric field in ISR2:

\[ E_{x4s} = \alpha(B - \Delta E_x), \]
\[ E_{y4s} = \alpha(C - \Delta E_y), \]

where \( \alpha \) is the amplitude correction factor due to the ambient electric field being “short-circuited” by the presence of the spacecraft and wire booms, see Sect. 4.1. And \( \Delta E_x \) (sunward offset) and \( \Delta E_y \) (duskward offset) are the ISR2 offsets, which represent the difference between the measured and geophysical electric fields in the despun frame and are discussed in detail later.

As the spin fitting procedure would typically yield different values for the electric field from the two different probe pairs, it is useful to introduce additional offset which describes the difference between the two measurements, \( \Delta p_{12p34} \), which we call the Delta offset:

\[ \Delta_{xp12p34} = E_{x4s}(E_{12}) - E_{x4s}(E_{34}), \]
\[ \Delta_{yp12p34} = E_{y4s}(E_{12}) - E_{y4s}(E_{34}). \]

The despun full resolution electric field is obtained as follows:

\[ E_x = Re[\varepsilon_{12}] - \Delta_{xp12p34} + Re[\varepsilon_{34}], \]
\[ E_y = Im[\varepsilon_{12}] - \Delta_{yp12p34} + Im[\varepsilon_{34}], \]

where \( \varepsilon_{12} = (E_{12} - \Delta_{raw12})e^{i\phi_{12}} \), \( \varepsilon_{34} = (E_{34} - \Delta_{raw34})e^{i\phi_{34}} \), and \( \phi_{12} = \phi_{34} + \pi/2 \) is the spin phase of probe 1 with respect to the sun; Raw data DC offset, \( \Delta_{raw} = \langle A \rangle \), is based on...
parameter $A$ of the fit (Eq. 1). Ideally, the DC level of the raw data should be zero, however small differences between the probe surfaces and in the electronics create a DC offset in the raw data. If not corrected, it shows up as a signal at the spin frequency in the despun electric field.

It must be noted that asymmetries due to the direction to the sun have the dominant contribution to the offsets, so that the following inequalities are typically satisfied:

$$\Delta E_x \gg \Delta E_y,$$

$$\Delta_{xp12p34} \gg \Delta_{yp12p34}.$$

4 Results

In this section we summarize the main results concerning the various offsets defined above. Raw data DC offset and delta offsets are obtained from spin fits, while the amplitude correction factor and ISR2 offsets are obtained based on inter-spacecraft calibration as well as cross-calibration with CIS (Reme et al., 2001) and EDI (Paschmann et al., 1997, 2001).

4.1 Amplitude factors

Amplitude factors are needed since the electric field is partially “short circuited” by the spacecraft potential, which is also the potential of the wire booms, extending out to a large distance from the spacecraft (Cully et al., 2007).

We have used the ISR2 Y components of the electric field to determine the amplitude correction factor. This component of $E$ is generally free from offsets and thus by comparing $E_y$ from EFW and CIS-HIA we are able to deduce the amplitude correction factor. Results of such computations for the spring season of 2002 are shown in Fig. 3. Every point in the plot corresponds to one orbit of data. One should mention that variations seen in the data are not caused by changes in the factor, but rather by “bad data” and insufficient data coverage.
On the basis of simulations and comparisons with other Cluster instruments it has been determined that the measured electric field magnitude needs to be multiplied by a factor of 1.1. We use this constant value through the entire mission. This value is consistent with valued obtained from simulations of the spacecraft-plasma interaction (Cully et al., 2007).

### 4.2 Raw data DC offset

The raw data DC offset, $\Delta_{\text{raw}}$, from the both probe pairs is used for calculate the full-resolution E-field. It is applied to $E_{12}$ and $E_{34}$ prior to despining. Variations in the electric field will result in small changes to A computed from spin fits for different 4 s intervals. So if $\Delta_{\text{raw}}$ depended only on the electronics, one could compute a long-term average of A and use it as $\Delta_{\text{raw}}$. But we find that A also depends on the surrounding plasma environment as illustrated in Fig. 4, where A is plotted as a function of the spacecraft potential. Therefore we want to a smoothened value and at the same time to track changes in the plasma environment. That is why the DC offset is smoothed, $\Delta_{\text{raw}} = \langle A \rangle$, using a weighted average over 7 spins using weights [0.07 0.15 0.18 0.2 0.18 0.15 0.07].

### 4.3 ISR2 offsets

Our main assumption in the study of ISR2 offsets is that the offsets depend on the instrument configuration, spacecraft attitude and that the dependence on surrounding plasma parameters is weak, i.e. being in the same kind of plasma environment (for example plasmasheet) and having the same instrument settings and probe properties for two different time intervals, the difference for between ISR2 offsets for the two intervals must be within the uncertainty of the offset determination (several tenth of mVm$^{-1}$). As the offsets still depend on the plasma environment we decided to split the dataset into two groups “solar wind/magnetosheath” and “magnetosphere” which correspond to two situations with “cold and dense” and “hot and rarefied” plasmas. To split every
For the solar wind/magnetosheath intervals, we first perform the inter-spacecraft calibration under assumption that all the spacecraft observe the same large-scale electric field, which is the case in the solar wind. As a result we get for each interval (from outbound magnetopause crossing to the inbound, typically several hours long) we get relative offset between the spacecraft, which are the differences in $E_x$ and $E_y$ between the different spacecraft averaged over the entire interval. Figure 5 shows an example of such interval, and the two upper panels show $E_x$ and $E_y$ from all four spacecraft.

Then by using CIS-HIA from C1 and/or C3 as reference data we find the ISR2 offsets for EFW for each of the spacecraft. We get one value for offsets per orbit. The procedure can be controlled visually by using a type of plot presented in Fig. 5. The two upper panels show all the available EFW and CIS-HIA data ($E_x$ and $E_y$ in ISR2). Then we construct the reference $E$-field from CIS-HIA by averaging data from the spacecraft where CIS-HIA data is available. Such averaging is possible as the difference between the spacecraft in the SW/MSH is typically small. Then we compute the difference between the EFW $E_x$ on all spacecraft and the reference $E$-field; this difference is plotted in the third panel. Average of the difference over the entire interval gives the local IRS2 offset. This offset is then applied to the EFW on different spacecraft. The resulted corrected and reference E-fields are plotted at the two bottom panels.

Evolution of ISR2 offsets in the solar wind and magnetosheath during mission lifetime is shown in Fig. 6. One can see that the offsets are rather steady and slowly decreasing with approach of the solar minimum ($\sim 2009$). The only striking feature is the sudden increase of the offset on C3 in 2005. This change is not yet understood.
4.3.2 ISR2 offsets in the magnetosphere

The problem of determining the offsets in the magnetosphere is significantly more complicated in comparison to the solar wind/magnetosheath. Data from the other instruments, which could have been used as a reference, is of very low quality in large areas of the magnetosphere due to low counts (the CIS instrument) or low magnetic fields (the EDI instrument). Also the EFW data are subject to frequent problems, such as electrostatic wakes, and the data affected by wakes needs to be excluded from the dataset used to determine the offsets.

In the ISR2 offset determination procedure we decided not to use any reference data, but rather use a condition of zero electric field $\langle E_x \rangle = 0$, as most of the times the electric fields are very weak in the magnetotail ($X_{GSE} < 0$ and $R > 5$ RE), and the averaged over a tail season must be very close to zero, and the difference from zero gives a rather good estimate for the ISR2 $E_x$ offset. The resulting offsets were verified against the CIS data for a large number of cases, and in particular in the central plasmasheet the agreement is very good.

Results for Cluster 4 for years 2002–2005 are summarized in Fig. 7. One can see that there is a prominent peak around 1.3 mV m$^{-1}$ for all years, however there is also some group of points giving rise to a broadening towards lower offsets values. Therefore we can conclude that the offset value is rather stable, and the broadening is due to actual geophysical electric fields present in the magnetosphere.

Evolution of ISR2 offsets in the magnetosphere during mission lifetime is shown in Fig. 8. The offsets are steady and slowly decreasing with approach of the solar minimum.

4.4 Delta offset

Given the two identical probe pairs we are able to estimate the electric field at the time scale of the spacecraft spin from each of them, and in principle these estimates should be identical. In reality the probes are not identical, and the estimates of the electric
fields differ. Such a difference is described by the Delta offset. Figure 9 shows how the Delta offsets change over time. The curves show the raw data, i.e. the difference between the electric fields computed from the two probe pairs averaged over 1.5 h-long intervals of data. One can see that the offset varies very slowly, at a typical time scale of several months, and with some sudden jumps typically related to spacecraft manoeuvres. Therefore for the calibration purposes we use a smoothened version of the offset, i.e. median over approximately two orbits. This approach allows us to get rid of the outliers, which can be caused by intervals with non-optimal instrument performance or strong geophysical electric fields.

Figure 10 shows the long-term evolution of the Delta offsets for all four spacecraft. Variations in the offset are caused by a number of factors. First is the solar cycle. One can see that the offset is rather small and steady in the beginning of the mission and starts to grow with approach of the solar minimum, reaching it’s maximum in spring 2006. This behaviour is caused by non-optimal bias current settings, and the situation got significantly improved by lowering the bias current in June 2006. The second cause is the probe failures, which forced usage of P32 (shorter base and asymmetric with respect to the spacecraft) instead of P12 (see Fig. 1).

5 Discussion and conclusions

Here we presented an overview of the calibration procedure used for the DC electric field measurements by EFW on Cluster, which is applied for production of the data for the Cluster Active Archive (CAA). EFW measures potential difference between probes mounted on long wire booms, which, after some corrections, can be used to construct the electric field in the spacecraft spin plane. We show that the calibration procedure leading to an estimate of the geophysical electric field can be described by a set of offsets, which are determined from the symmetry considerations enabled by rapid spacecraft spin as well as from statistical comparisons with other measurements of the elec-
electric field on Cluster. We show that most of the offsets have a rather slow variation with time on time scales of weeks and month.

We should note that the presented approach is not capable of correcting for fast changes of the offsets caused by for example by rapid crossing of plasma boundaries such as the bow shock and magnetopause. At present calibration of such events usually requires manual calibration if precision on the DC electric field below 1 mV m$^{-1}$ is required, and reliable calibration is only possible when all probes respond to changes in the plasma environment in a very similar way and the effect of this changes on offsets is not too drastic. Developing a procedure, which would produce reliable results also for such cases during routine data production, remains a challenging task.

As a concluding remark, we note that the described calibration procedure applies to data acquired when the instrument operates close its optimal regime, so that one can reconstruct the ambient electric field present in the plasma by applying relatively small corrections. However, a major effort during the CAA production goes into detection of strong deviations from the nominal operations (Khotyaintsev et al., 2010), which can be caused by both changes of the plasma environment surrounding the spacecraft and non-optimal instrument settings.

Acknowledgements. The authors thank their colleagues for continuing support and discussion around the coffee breaks.

References


Fig. 1. Cluster EFW double-probe electric field instrument.
Fig. 2. Raw data of the electric field, $E_{12}, E_{34}$ (upper panel) and of the probe-to-spacecraft potential $P_1, P_2, P_3, P_4$, (bottom panel) measured by Cluster 1.
Fig. 3. Amplitude correction factor for the electric field measured by EFW on cluster 1–4 during a solar wind season from November 2002 to June 2003.
Fig. 4. Dependence of the raw data DC offset, $\Delta_{\text{raw}}$, computed from the spin fits on the spacecraft potential showing that the offset decreases when the potential is close to zero (characteristic of dense plasmas).
Fig. 5. Inter-spacecraft calibration and cross-calibration with CIS in the solar wind/magnetosheath. Panels from top to bottom show $E_x$ and $E_y$ measured by EFW on the 4 spacecraft and by CIS-HIA on C1 and C3, difference in $E_x$ between CIS and EFW (median value from all spacecraft), the spacecraft potential, and the two bottom panels show the same data as on the top, but with the offsets applied to the EFW data. Data from the four Cluster spacecraft shown by black (C1), red (C2), green (C3) and blue (C4).
Fig. 6. Long-term evolution of the ISR2 $E_x$ (sunward) offset in the Solar wind/magnetosheath from 2001 to 2009.
Fig. 7. Probability distribution function of ISR2 $E_x$ (sunward) offset for Cluster 4 in the magnetosphere for 2002–2005.
Fig. 8. Long-term evolution of the ISR2 offsets in the magnetosphere from 2001 to 2009.
Fig. 9. Evolution of the “raw” Delta offsets on Cluster 1–4 from 2001 to 2005. The blue and green lines show $X$ and $Y$ components of the difference between the electric fields computed from the different probe pairs, i.e. the “raw” delta offsets. In order to get rid of the outliers (spikes), we compute the median of this difference, which is then used as the delta offset applied to data during the calibration process.
Fig. 10. Long-term evolution of delta offsets from 2001 to 2009 for C1 (black), C2 (red), C3 (green) and C4 (blue).